

LAMBERT'S LAW:

"When a beam of monochromatic radiation passes through a homogenous absorbing medium, the rate of decrease of intensity of radiation with thickness of absorbing medium is proportional to the intensity of incident radiation."

$$\frac{-dI}{dx} \propto kI$$

I = intensity of radiation after passing through thickness x of medium.

$\frac{-dI}{dx}$ = rate of decrease of intensity of radiation with thickness of the absorbing medium.

k = absorption coefficient.

Let I_0 be intensity of radiation before entering the absorbing medium ($x=0$), and I be intensity of radiation after passing through thickness, x of medium.

$$\frac{-dI}{dx} = kI \Rightarrow \frac{dI}{I} = -kdx$$

$$\int_{I_0}^I \frac{dI}{I} = - \int_{x=0}^{x=x} k dx \Rightarrow \ln \frac{I}{I_0} = -kx \Rightarrow \frac{I}{I_0} = e^{-kx}$$

$$I = I_0 e^{-kx} \quad \text{--- (1)} \Rightarrow I = I_0 10^{-ax} \quad \left[a = \frac{k}{2.303} \right]$$

Intensity of radiation absorbed,

$$I_{\text{abs}} = I_0 - I = I_0 - I_0 e^{-kx} \quad (\text{By eqn. (1)}) \\ = I_0 (1 - e^{-kx})$$

- BEER'S LAW:

'when a beam of monochromatic radiation is passed through a sol¹ of an absorbing substance, the rate of decrease of intensity of radiation with thickness of the absorbing sol¹ is proportional to the intensity of incident radiation as well as the concentration of the sol¹'

$$-\frac{dI}{dx} = k' I c$$

where c = conc. of sol¹ (moles/l)

k' = molar absorption coefficient
(depends upon nature of absorbing surface)

$$\int_{I_0}^I \frac{dI}{I} = - \int_{x=0}^{x=x} k' c dx$$

$$I = I_0 e^{-k' cx}$$

By changing the logarithm to base 10, $I = I_0 \cdot 10^{-\alpha' cx}$

$$\frac{k'}{2.303} = \alpha', \alpha' = \text{molar extinction coefficient of absorbing sol}^1$$

Beer's law can also be stated as:

when a monochromatic light is passed through a sol¹ of an absorbing substance, its absorption remain constant when the conc(c) and the thickness of the absorption layer(r) are changed in the inverse ratio.

On combining the two laws, Beer-Lambert Law :

$$\log \frac{I_0}{I} \cdot E.C. l = A$$

where,

I_0 = intensity of incident light

I = Intensity of transmitted light

C = conc. of solⁿ (molar/l)

l = Path length of the sample (usually 1 cm)

ϵ = molar absorptivity / molar extinction coefficient
 $FL/mol \cdot cm$

A = Absorbance

Limitations of Beer Lambert Law - This law is not obeyed.

- i) In keto-enol tautomers
- ii) in fluorescent compounds
- iii) when solute and solvent form complexes.